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# THE GPS BROADCAST ORBITS: AN ACCURACY ANALYSIS

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# Outline



- Motivation
- Goals
- Approach
- Results
- Web Display
- U.S. Space Command Reports
- Anticipated Broadcast Orbit Improvements
- Conclusions and Future Work



# Motivation



- Day-to-day accuracy of navigation message ephemerides (broadcast orbits) not readily available
- Independent assessment of ephemeris error in Standard Positioning Service error budget considered useful
- Broadcast orbit accuracies needed to assess errors in future U.S. and Canadian Wide Area Augmentation Systems (WAASs)



# Goals



- Develop algorithms and software to automatically compute (once per day) the broadcast orbit errors and meaningful statistics
- Develop algorithms and software to automatically compute (once per day) the WAAS orbit correction errors and meaningful statistics
- Post the analysis results on the World Wide Web



# Approach



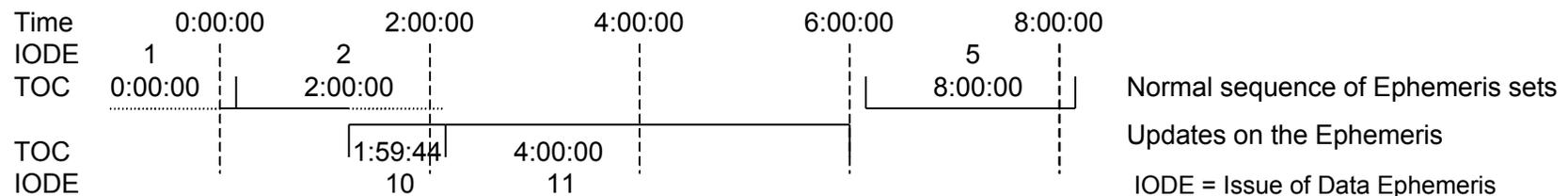
- Accuracies are assessed through comparisons with orbit products provided by the International GPS Service (IGS)
- Separate assessments carried out with IGS predicted, rapid, and final orbits
- Broadcast orbits obtained from “auto” RINEX navigation files provided by Scripps Orbit and Permanent Array Center (SOPAC) Web site
- IGS orbits obtained from the IGS Central Bureau ftp site



# Approach, cont'd.



- Broadcast orbits evaluated according to ICD-GPS-200
- Ephemeris sets are normally updated every 2 hours
- Ephemeris set considered valid from 2 hours before Time of Ephemeris (TOE) until 2 hours after TOE
- But a particular set is first used when it was first transmitted = Transmission Time of Message (TTOM), typically 1:59:42 before TOE





# Approach, cont'd.



- Antenna phase centre offset from spacecraft centre of mass:

Block II/IIA\*:  $x_{pc} = 0.279$ ,  $y_{pc} = 0.000$ ,  $z_{pc} = 1.023$  metres

Block IIR\*:  $x_{pc} = 0.279$ ,  $y_{pc} = 0.000$ ,  $z_{pc} = 1.023$  metres

- Standard body-fixed frame to WGS 84 conversion applied
- No datum transformation; WGS 84 assumed consistent with IGS frame (ITRF)

\*NIMA uses

Block II/IIA\*:  $x_{pc} = 0.2794$ ,  $y_{pc} = 0.0000$ ,  $z_{pc} = 0.9519$  metres

Block IIR\*:  $x_{pc} = 0.0000$ ,  $y_{pc} = 0.0000$ ,  $z_{pc} = 1.1725$  metres



## Approach, cont'd.



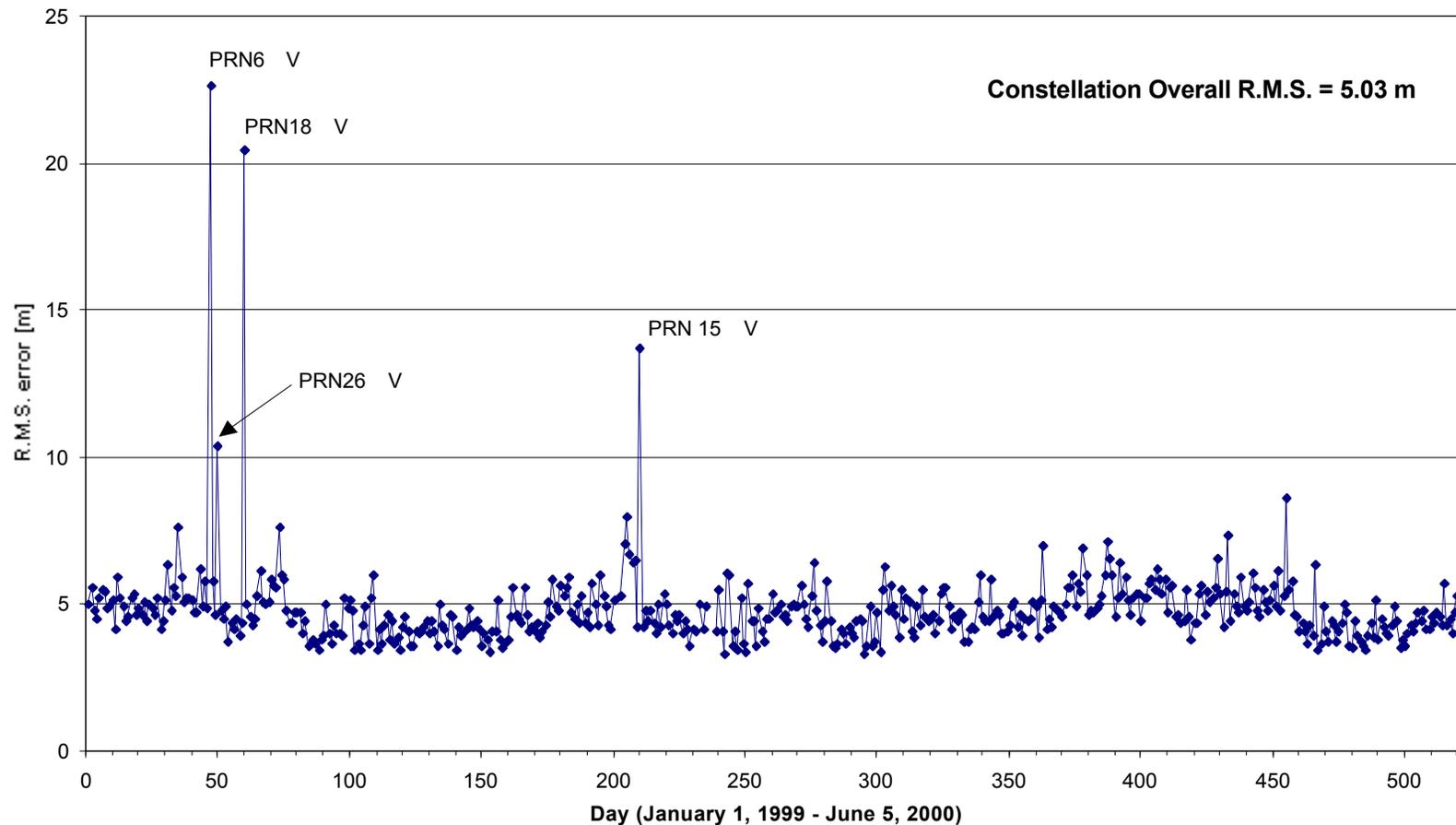
- Broadcast orbits computed every 15 minutes at the IGS orbit epochs
- Differences between broadcast orbit x, y, z values and IGS values computed = dx, dy, dz
- For each day, the minimum, maximum, and r.m.s. differences, dx, dy, dz for each satellite are computed
- 3D-error:  $\sqrt{dx^2 + dy^2 + dz^2}$  also computed
- Results posted to Web



# Constellation Daily 3D R.M.S. Error



Broadcast orbit R.M.S. error with respect to IGS final orbit  
(constellation 3D R.M.S.)





# Some Problem Satellites

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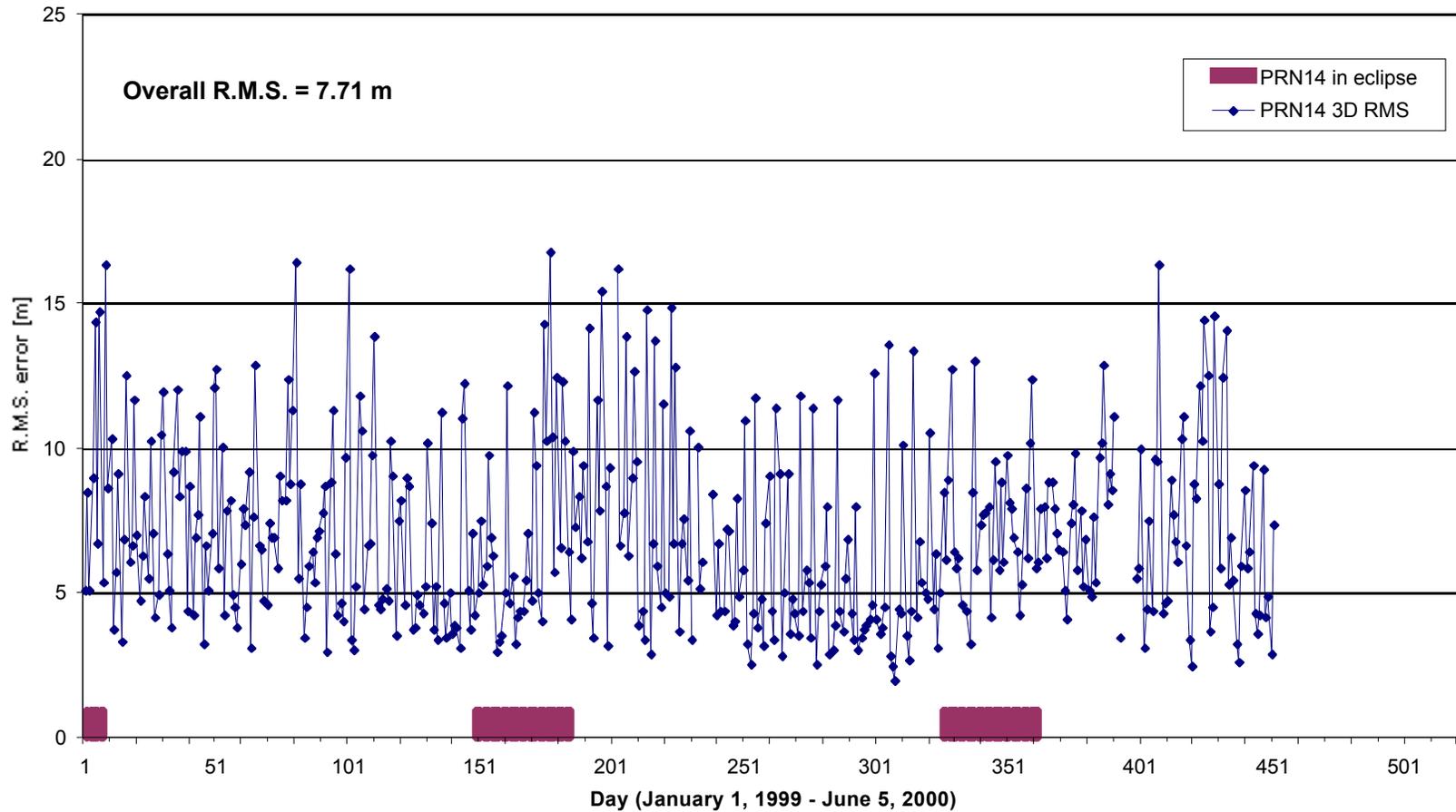
- PRN02 - possible problems in eclipse
- PRN14 - large ranging errors; retired 14/4/00
- PRN15 - reaction wheel problems in eclipse
- PRN16 - clock problems
- PRN18 - reaction wheel problems in eclipse
- PRN23 - solar array slewing in eclipse



# PRN14 Daily 3D R.M.S. Error



PRN 14 broadcast orbit R.M.S. error with respect to IGS final orbit  
(3D R.M.S.)

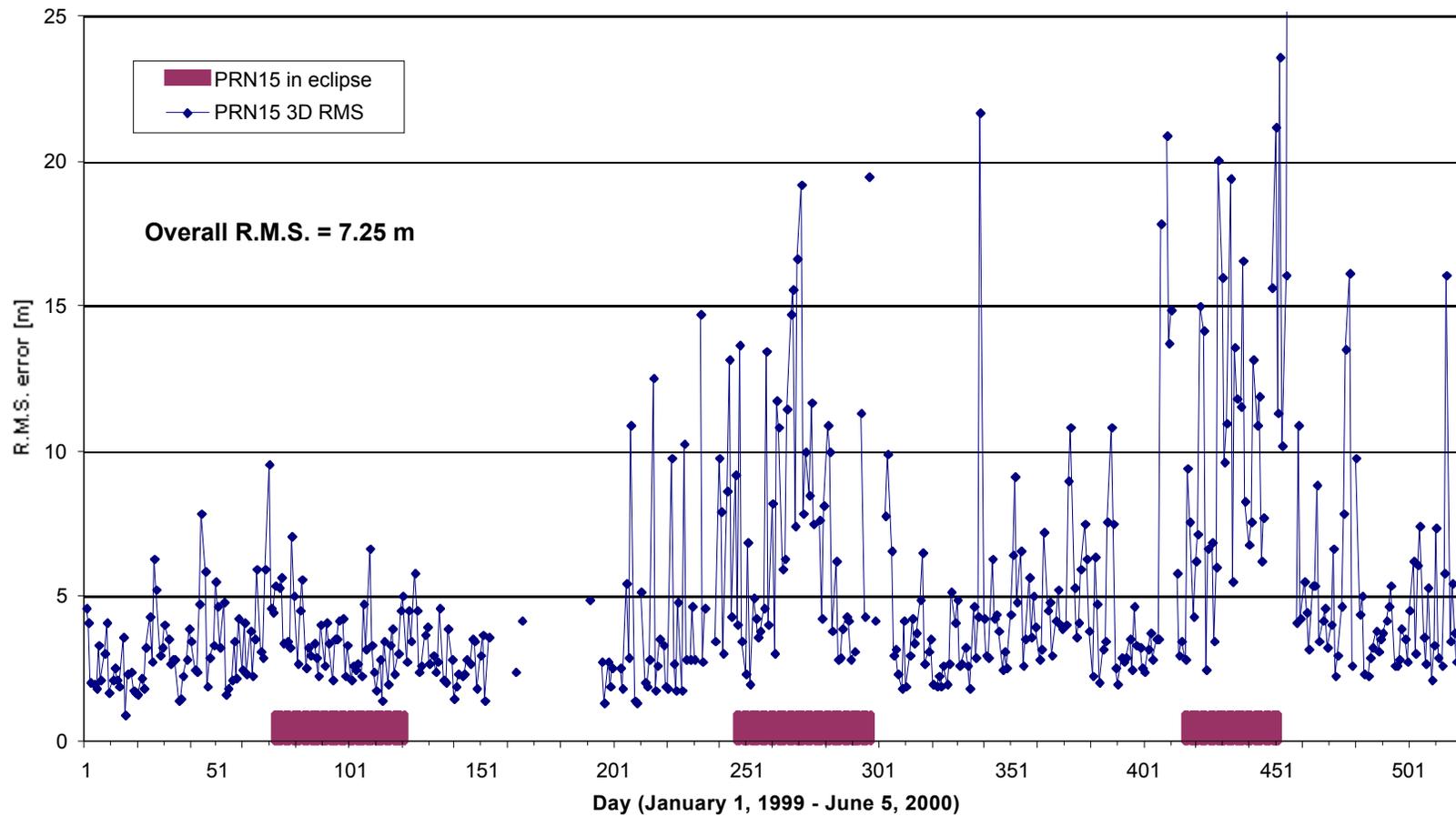




# PRN15 Daily 3D R.M.S. Error



PRN 15 broadcast orbit R.M.S. error with respect to IGS final orbit  
(3D R.M.S.)

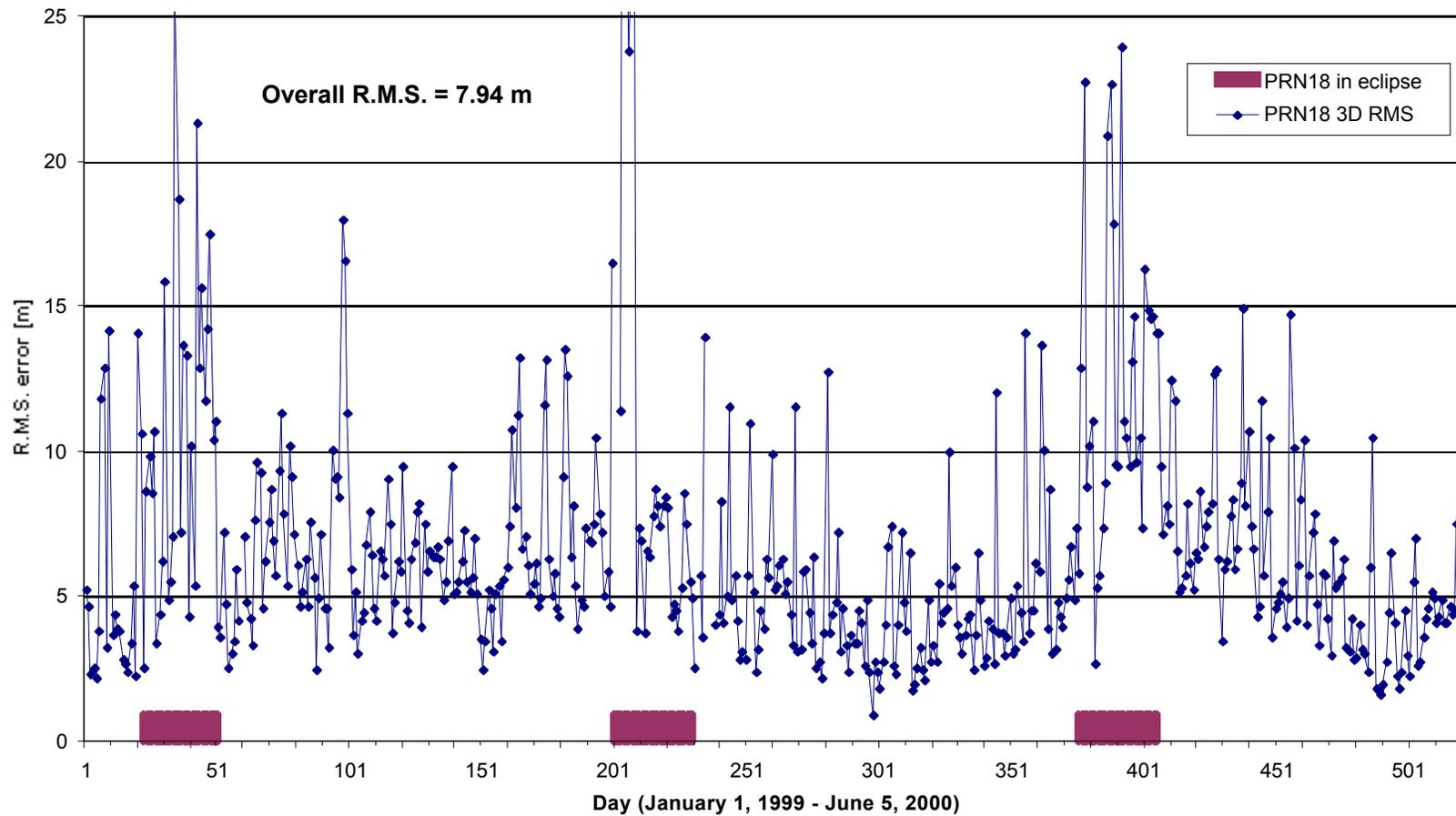




# PRN18 Daily 3D R.M.S. Error



PRN 18 broadcast orbit R.M.S. error with respect to IGS final orbit  
(3D R.M.S.)

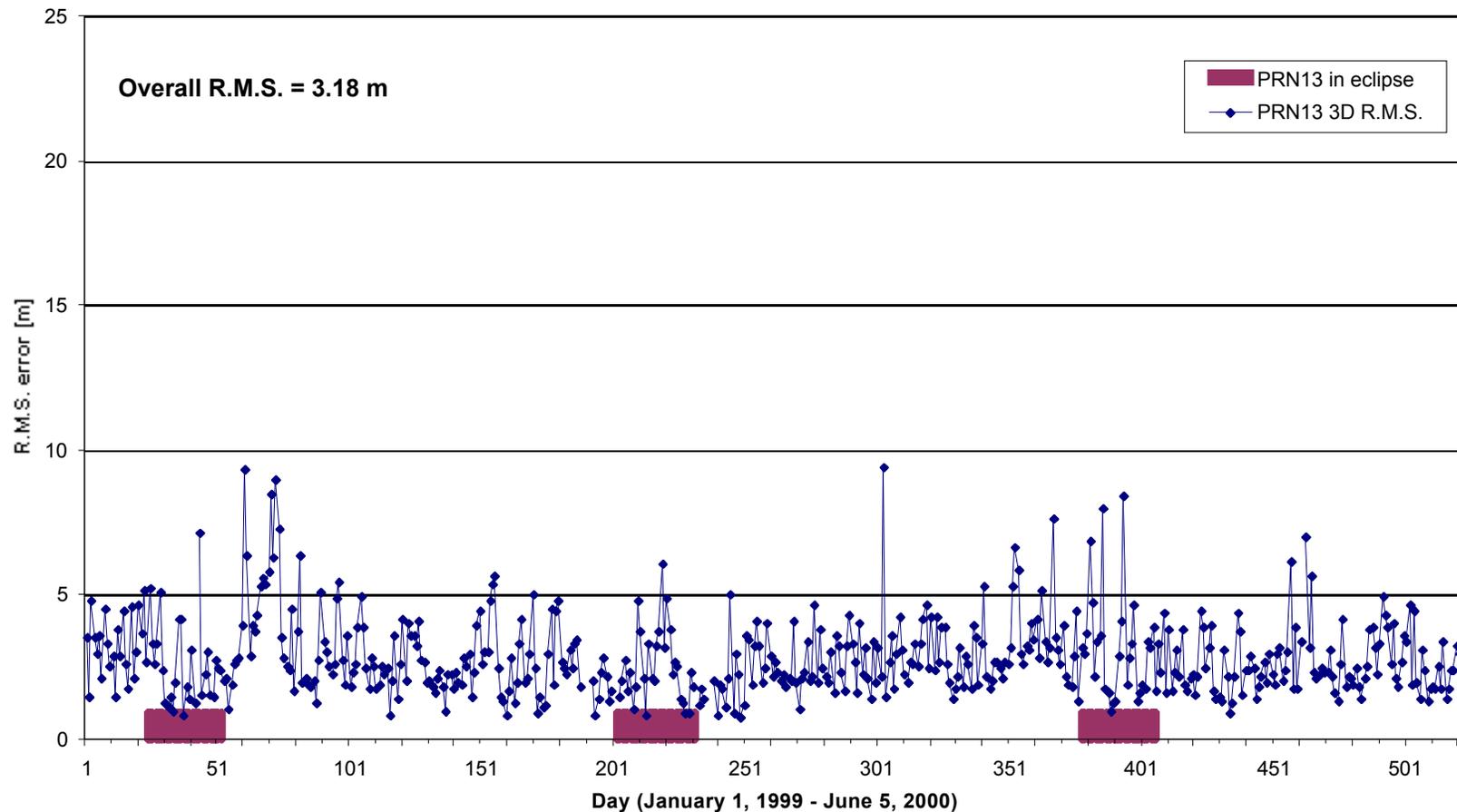




# PRN13 Daily 3D R.M.S. Error



PRN 13 broadcast orbit R.M.S. error with respect to IGS final orbit  
(3D R.M.S.)

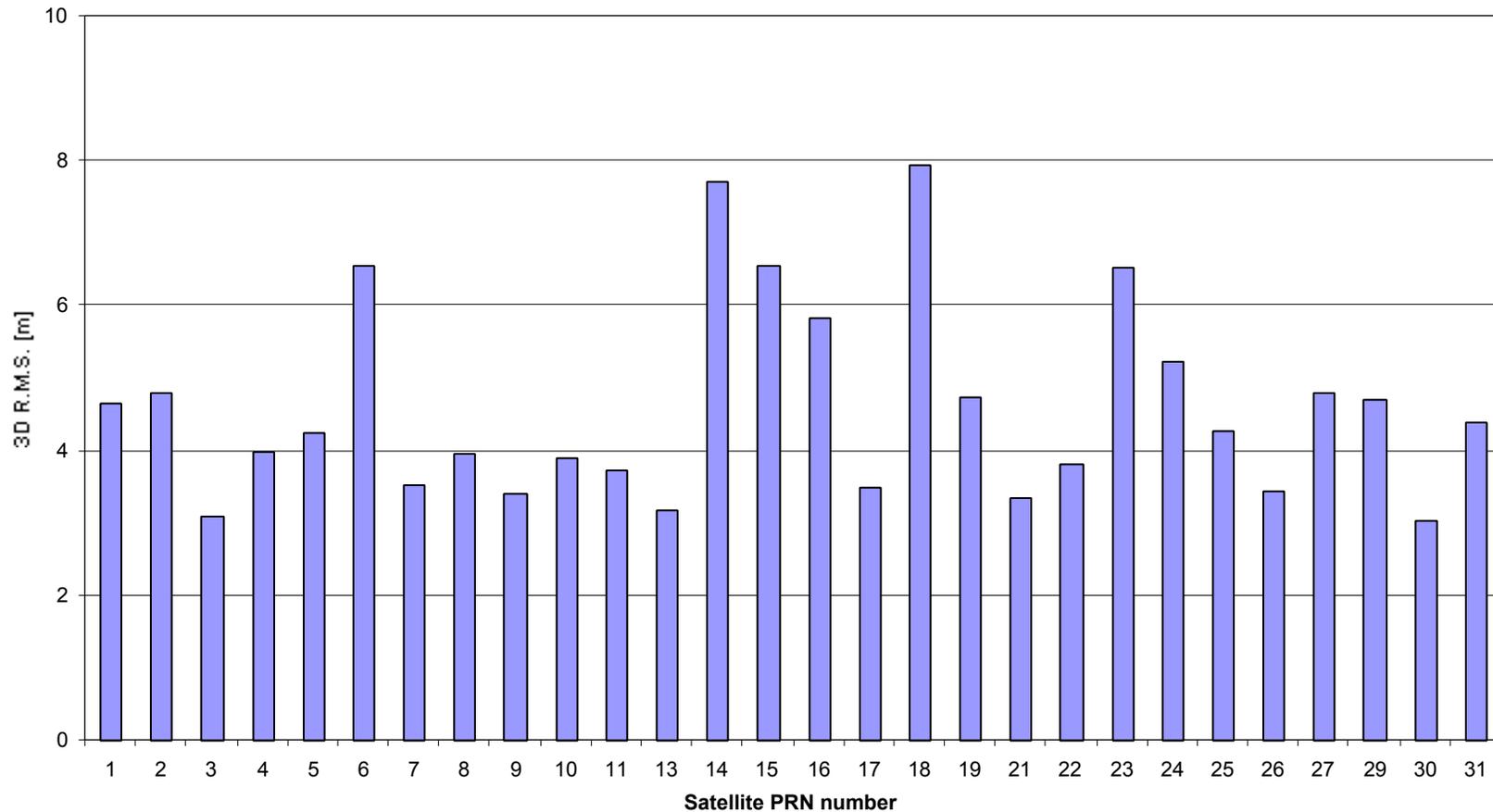




# 3D R.M.S. Error by Satellite



Broadcast orbit R.M.S. error with respect to IGS final orbit  
(January 1, 1999 - June 5, 2000)

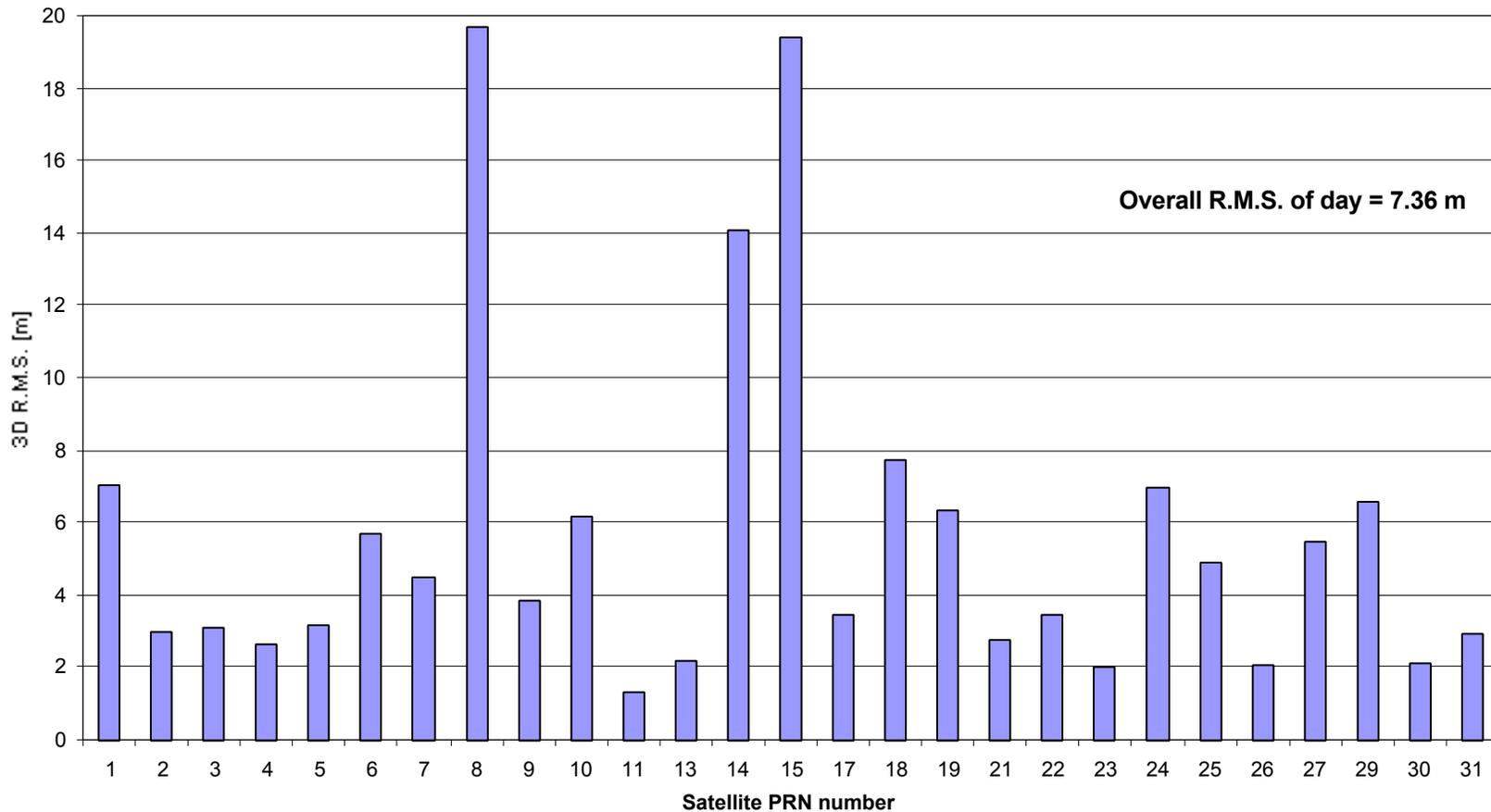




# 3D R.M.S. Error on March 8, 2000



Broadcast orbit R.M.S. error with respect to IGS final orbit  
(March 8, 2000)

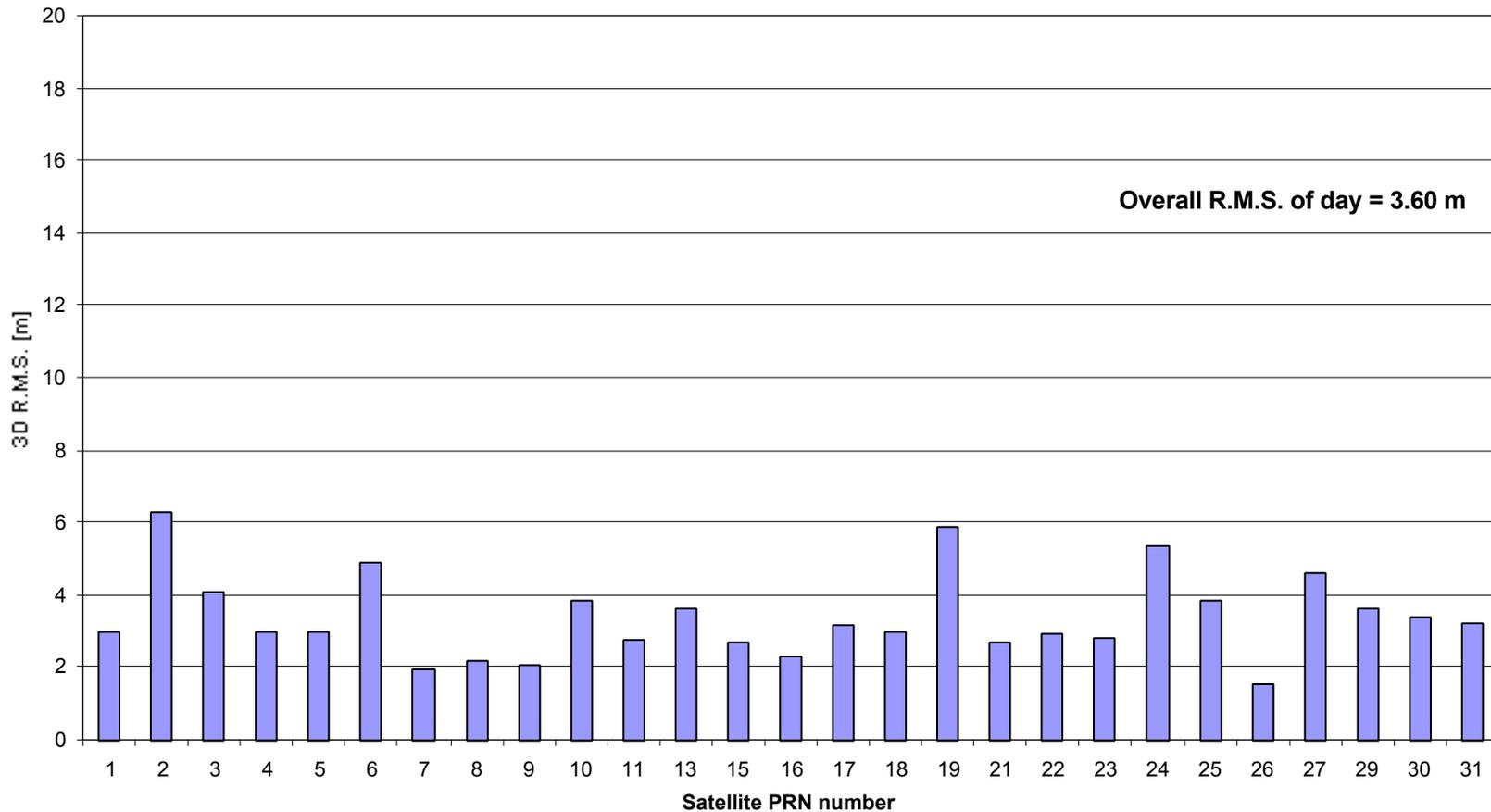




# 3D R.M.S. Error on May 14, 2000



Broadcast orbit R.M.S. error with respect to IGS final orbit  
(May 14, 2000)

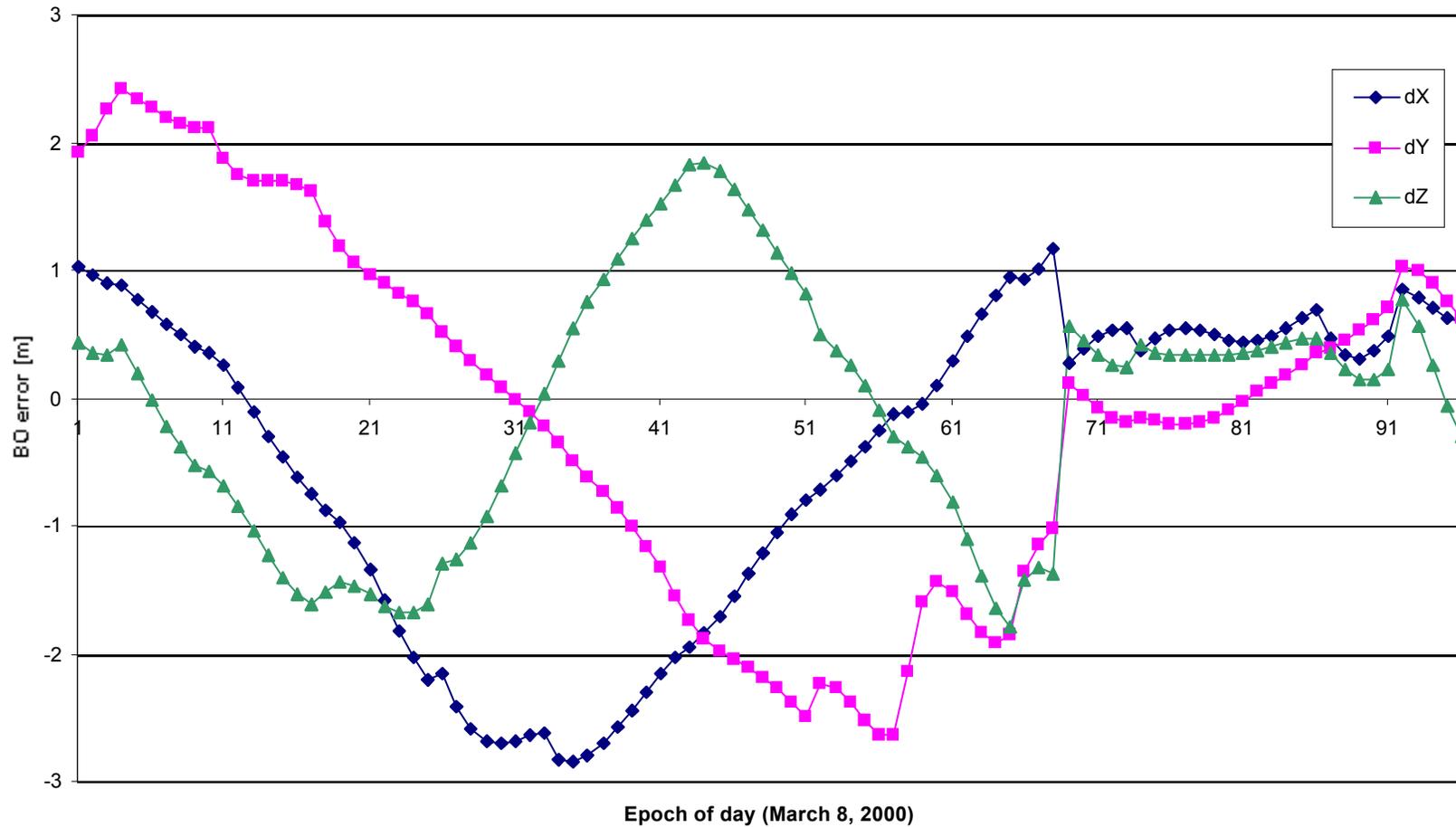




# PRN13 XYZ Errors on March 8, 2000



PRN 13 - Broadcast orbit error with respect to IGS final orbit

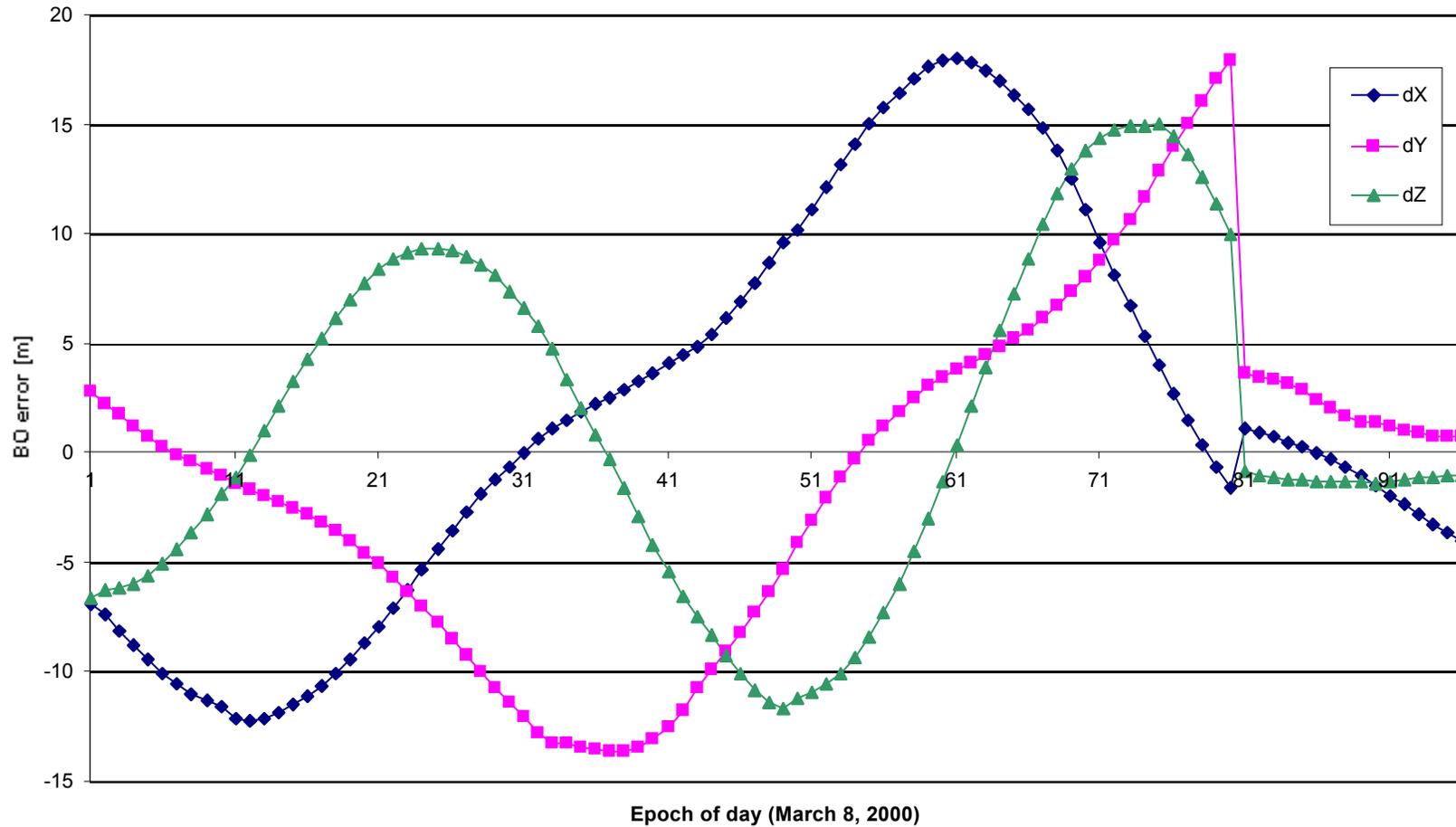




# PRN14 XYZ Errors on March 8, 2000



PRN 14 - Broadcast orbit error with respect to IGS final orbit

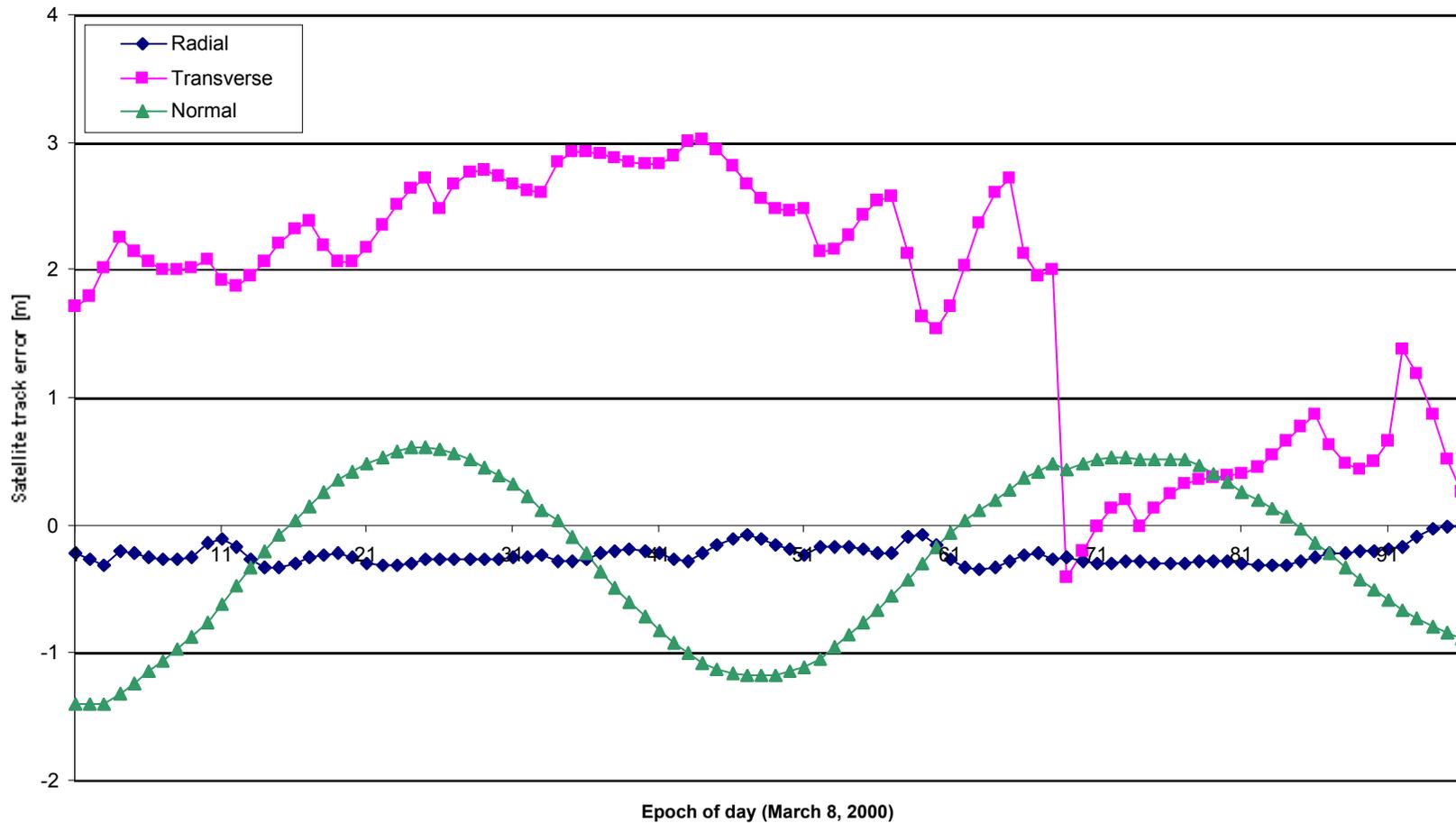




# PRN13 RTN Errors on March 8, 2000



PRN 13 - Transformed broadcast orbit error with respect to IGS final orbit

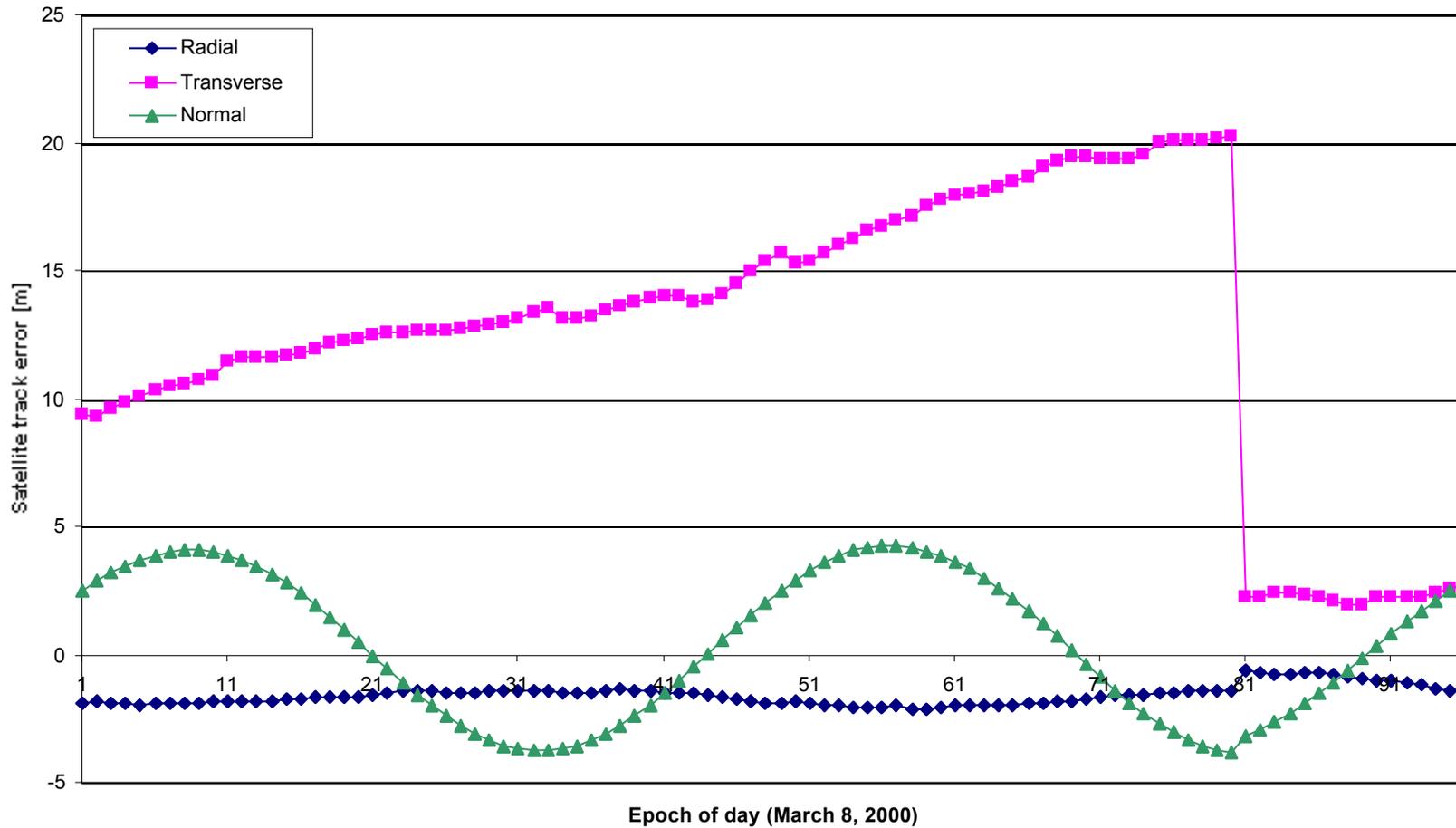




# PRN14 RTN Errors on March 8, 2000



PRN 14 - Transformed broadcast orbit error with respect to IGS final orbit





# Web Display



The screenshot shows a Netscape browser window with the address bar containing `http://gauss.gge.unb.ca/grads/orbit/`. The page content is as follows:

University of New Brunswick, Department of Geodesy and Geomatics Engineering, GPS Lab

## Welcome to the GPS Lab

These pages show the daily statistics of the accuracy of the GPS Broadcast Ephemeris (Broadcast Orbit) and the WAAS-corrected Orbit.

Choose the desired orbit type (Broadcast Orbit or WAAS-corrected Orbit), enter the date and choose the comparison orbit. After pressing the "Show table"-Button you will see the statistics.

Keep in mind that the statistics become available with a delay of 2 days due to the availability of the IGS Rapid Orbit. Comparisons with the IGS Final Orbit (more accurate) become available with a delay of 20 days.

**Navigation Links:**

- Welcome
- Accuracy
  - Broadcast orbit
  - WAAS orbit
- Information
  - Calculation
  - What is WAAS?
- Contact



# Web Display cont'd.



The screenshot shows a Netscape browser window with the address bar containing `http://gauss.gge.unb.ca/grads/orbit/`. The page content is as follows:

University of New Brunswick, Department of Geodesy and Geomatics Engineering, GPS Lab

**GPS broadcast orbit accuracy statistics**

Day:   
Month:   
Year:

**Compared with IGS orbit:**

- Final orbit
- Rapid orbit
- Predicted orbit

On the left side of the page, there is a navigation menu with the following links:

- Welcome
- Accuracy
  - [Broadcast orbit](#)
  - [WAAS orbit](#)
- Information
  - [Calculation](#)
  - [What is WAAS?](#)
- Contact



# Web Display cont'd.

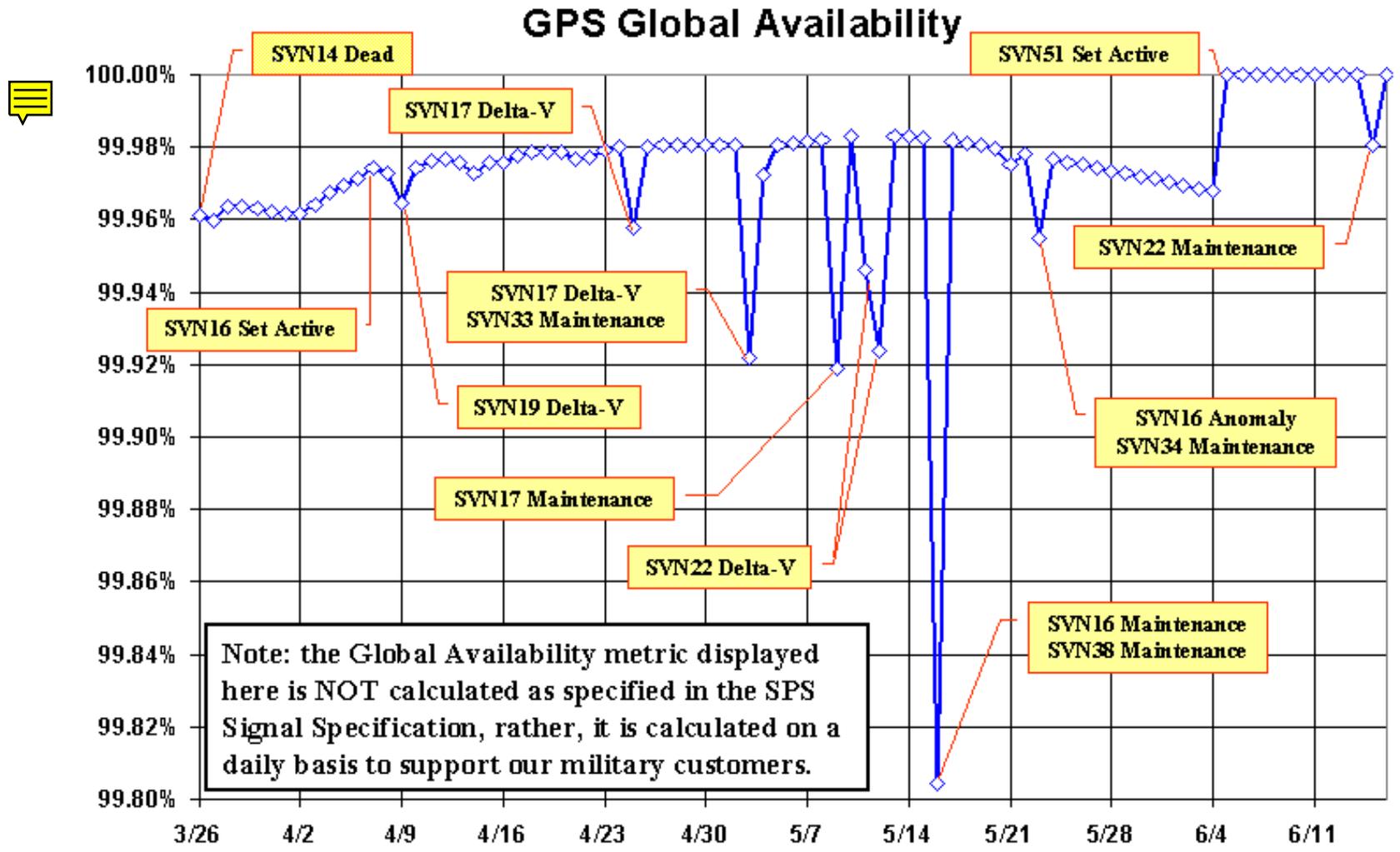


University of New Brunswick, Department of Geodesy and Geomatics Engineering, GPS Lab

## GPS broadcast ephemeris accuracy statistics (compared with IGS final orbit)

Year 2000, Day 068  
Overall R.M.S. = 7.36 m

PRN	X [m]			Y [m]			Z [m]			3D [m]		
	min	max	r.m.s	min	max	r.m.s	min	max	r.m.s	min	max	r.m.s
1	-8.111	6.122	3.464	-8.208	9.921	4.151	-11.069	7.331	4.540	1.242	14.727	7.060
2	-1.927	3.388	1.076	-3.241	4.296	2.041	-6.227	0.296	1.927	0.564	7.541	3.006
3	-3.612	3.899	2.317	-3.839	2.007	1.578	-2.812	1.686	1.408	1.190	4.829	3.137
4	-2.747	3.051	1.831	-2.262	2.529	1.467	-2.160	3.447	1.195	1.250	4.371	2.633
5	-4.001	3.844	2.158	-3.211	3.218	1.910	-2.514	1.813	1.380	1.327	5.361	3.195
6	-5.986	7.793	3.742	-8.440	4.773	3.252	-2.349	5.179	2.808	1.349	9.265	5.698
7	-6.133	3.593	3.018	-4.944	3.886	2.665	-3.860	4.224	2.084	1.830	6.344	4.534
8	-42.671	4.207	11.489	-5.830	31.321	12.096	-6.670	33.952	10.458	1.364	52.937	19.690
9	-6.301	5.128	3.210	-2.380	1.328	0.844	-3.401	3.403	1.971	0.914	6.406	3.860
10	-6.925	7.843	4.478	-6.264	5.506	3.805	-2.106	4.952	1.967	4.242	9.224	6.197
11	-1.024	1.162	0.582	-1.374	1.505	0.747	-1.599	1.522	0.916	0.474	1.969	1.317





# Signal-in-Space Range Error



- Computed by GPS Control Segment
- Clock and ephemeris errors:

$$\text{SISRE} = \sqrt{(\text{R} - \text{CLK})^2 + \frac{1}{49} (\text{A}^2 + \text{C}^2)}$$

where

R = radial ephemeris error

A = along-track ephemeris error

C = cross-track ephemeris error

CLK = clock error



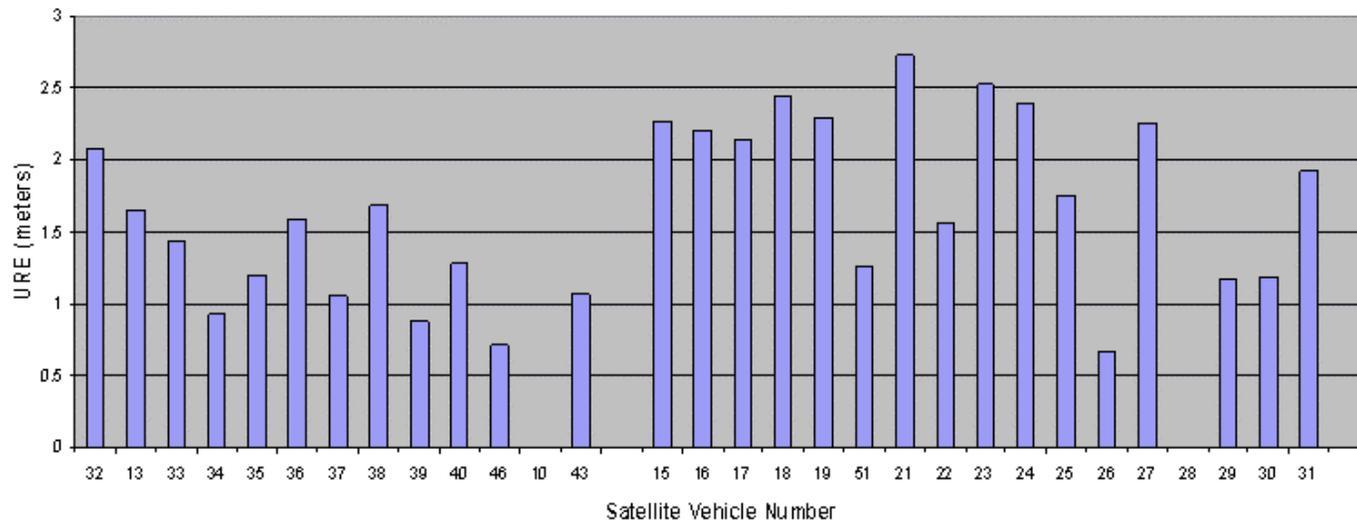
# Signal-in-Space Range Error Estimates



## UNCLASSIFIED *User Range Error Assessments*



Signal in Space User Range Error (URE)



20 June, 2000

UNCLASSIFIED



# Anticipated Broadcast Orbit Improvements



- Broadcast orbits should improve due to the GPS Accuracy Improvement Initiative (AII) and other efforts:
  - augment tracking network with NIMA stations
  - improve Master Control Station Kalman filter
  - more frequent uploads
  - expected r.m.s. SISRE after AII = 1.3 metres
  - further enhancements from clock replacements at monitor stations, multipath mitigation, improved tropospheric delay modelling, more satellites with rubidium clocks



# Conclusions and Future Work

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- Daily broadcast orbit error automatically computed and posted to the Web
- Database available for detailed study
- Constellation 3D r.m.s. error over past 18 months about 5 metres; some satellites as good as 3 metres
- RTN error components to be computed and compared to MCS SISRE estimates
- Comparison with NIMA precise ephemeris
- WAAS orbit correction errors to be assessed